

7.6 Vertex Form of the Quadratic Function $y = a(x - h)^2 + k$ or $y = a(x - p)^2 + q$ **Concept #11, 12**

VERTEX-GRAPHING FORM

Foundations 20 textbook uses: $y = a(x - h)^2 + k$ or Pre- Calculus 20 textbook uses: $y = a(x - p)^2 + q$

- the vertex is at (p, q) or (h, q)
 - if $a > 0$ (is positive), the parabola opens up
 - if $a < 0$ (is negative), the parabola opens down
 - the equation of the axis of symmetry is $x = h$ or $x = p$
- Note: $a \neq 0$

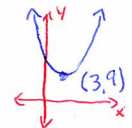
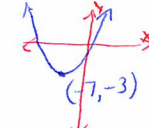
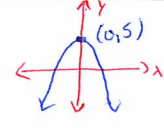
The graph of the function can be sketched more easily using this form.

Example1: For each quadratic function below, identify the following: **(CONCEPT #11)**

a) $f(x) = (x - 3)^2 + 9$

b) $m(x) = 2(x + 7)^2 - 3$

c) $r(x) = -2x^2 + 5$

i) Does the parabola open up or down? Max or Min?	up Min at $y = 9$	up Min at $y = -3$	down Max $y = 5$
ii) Coordinates of the vertex	$(3, 9)$	$(-7, -3)$	$(0, 5)$
iii) Equation of axis of symmetry	$x = 3$	$x = -7$	$x = 0$
iv) Domain	$D = \{x x \in \mathbb{R}\}$	$D = \{x x \in \mathbb{R}\}$	$D = \{x x \in \mathbb{R}\}$
v) Range	$R = \{y y \geq 9, y \in \mathbb{R}\}$	$R = \{y y \geq -3, y \in \mathbb{R}\}$	$R = \{y y \leq 5, y \in \mathbb{R}\}$
vi) How many zeros the function will have?	None 	Two 	Two 
vi) x and y-intercepts (Solve the x-int. using the square root property)	No x-intercepts y-int = $y = (0 - 3)^2 + 9$ Set $x = 0$ and solve $y = (9) + 9$ $y = 18$ $y\text{-int} = (0, 18)$	X-int set $y = 0$ and solve using the square root property $0 = 2(x + 7)^2 - 3 + 3$ get $(x+7)^2$ by itself $3 = \frac{2(x+7)^2}{2}$ $\pm \sqrt{\frac{3}{2}} = \sqrt{(x+7)^2}$ $\pm \sqrt{\frac{3}{2}} - 7 = x$ xintercepts y-int. $y = 2(0+7)^2 - 3$ $y = 2(49) - 3$ $y = 98 - 3$ $y = 95$ $y\text{-int} = (0, 95)$	X-intercepts $0 = -2x^2 + 5 - 5$ $-5 = -2x^2$ $\frac{-5}{-2} = \frac{-2x^2}{-2}$ $\sqrt{\frac{5}{2}} = \sqrt{x^2}$ $\pm \sqrt{\frac{5}{2}} = x$ xintercepts y-intercept $y = -2(0)^2 + 5$ $y = 5$ $y\text{-int} = (0, 5)$

Example 2: Sketch the graph of the following function: $f(x) = 2(x - 3)^2 - 4$ & State the domain and range. **Concept #11**

- Which way does it open? *UP*
- Where is the vertex? $(3, -4)$
- Where is the axis of symmetry? $x = 3$
- What are the x- intercepts?

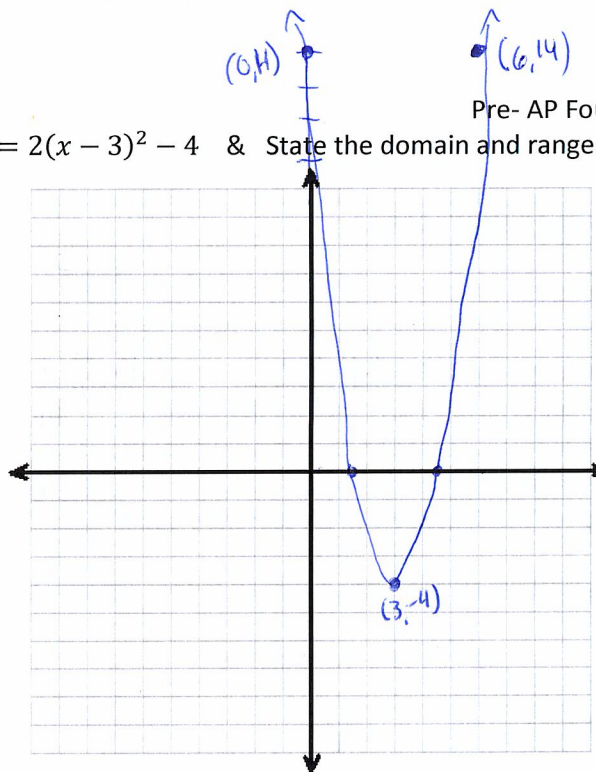
set $y=0$ or $f(x)=0$
 $0 = 2(x-3)^2 - 4 + 4$ *"Get the squared term by itself"*
 $4 = 2(x-3)^2$

$\frac{4}{2} = \frac{2(x-3)^2}{2}$
 $\sqrt{2} = \sqrt{(x-3)^2}$
 $\pm\sqrt{2} = x-3$
 $x = \{ \pm\sqrt{2} + 3 \}$

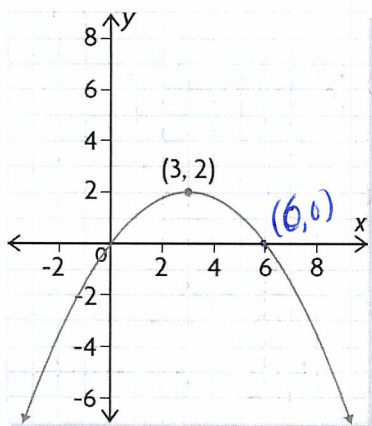
- What is the y-intercept? $\approx 4.4, 1.585$

- Reflect this point about the axis of symmetry to find the y intercepts reflection point

set $x=0$
 $y\text{-int} = y = 2(0-3)^2 - 4$
 $y = 2(-3)^2 - 4$
 $y = 2(9) - 4$
 $y = 18 - 4$
 $y = 14$
 $(0, 14)$



Example 3: Determine the equation of the quadratic function in vertex form **(Concept #12)**



Point
 $(6, 0)$
x y

$y = a(x-p)^2 + q$
 $y = a(x-3)^2 + 2$
 Point $(6, 0)$
 $0 = a(6-3)^2 + 2$
 $0 = a(3)^2 + 2 - 2$
 $-2 = \frac{9a}{9}$
 $-\frac{2}{9} = a$

$y = -\frac{2}{9}(x-3)^2 + 2$